

# *Papermaking Science and Technology*

a book series  
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future trends

*Book 16*

# Paper Physics

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